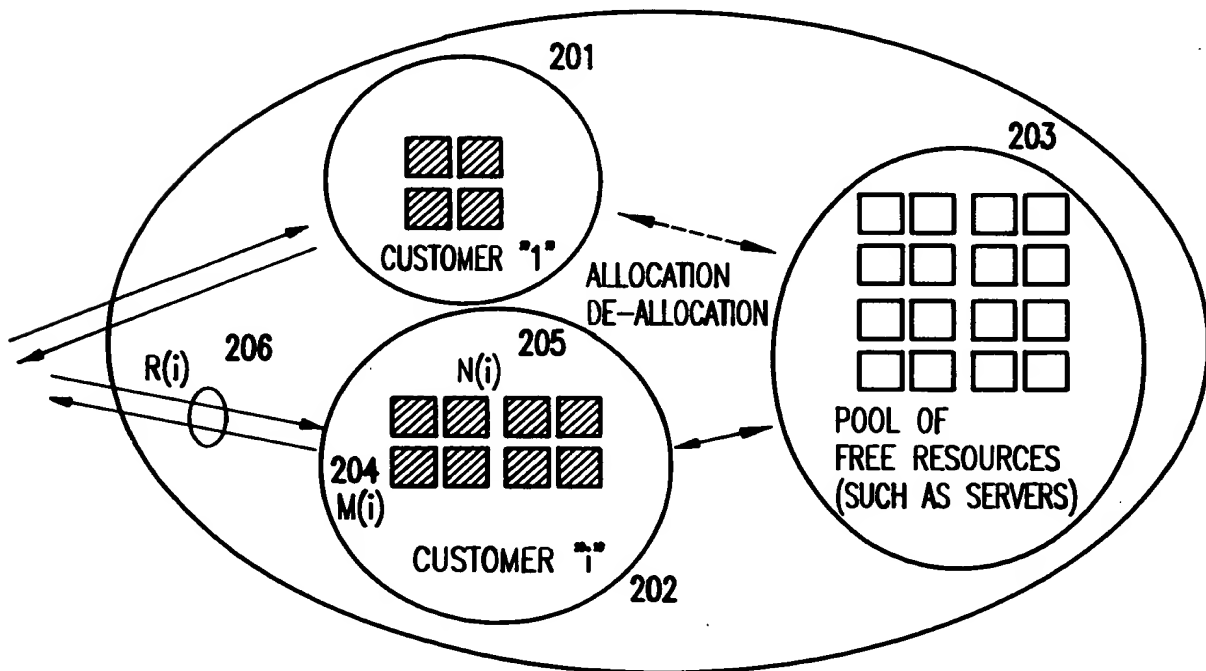


FIG. 1



MEASURE  $R(i)$ ,  $N(i)$ , AND  $M(i)$   
 COMPUTE  $N_t(i)$  AND  $R_t(i)$  FROM  $M_t(i)$ ,  $R(i)$ ,  $N(i)$  AND  $M(i)$ ,  
 AND THEN IF NEEDED, MOVE  $M(i)$  TO  $M_t(i)$  BY EITHER CHANGING  $N(i)$   
 TO  $N_t(i)$  OR CHANGING  $R(i)$  TO  $R_t(i)$ .

FIG. 2

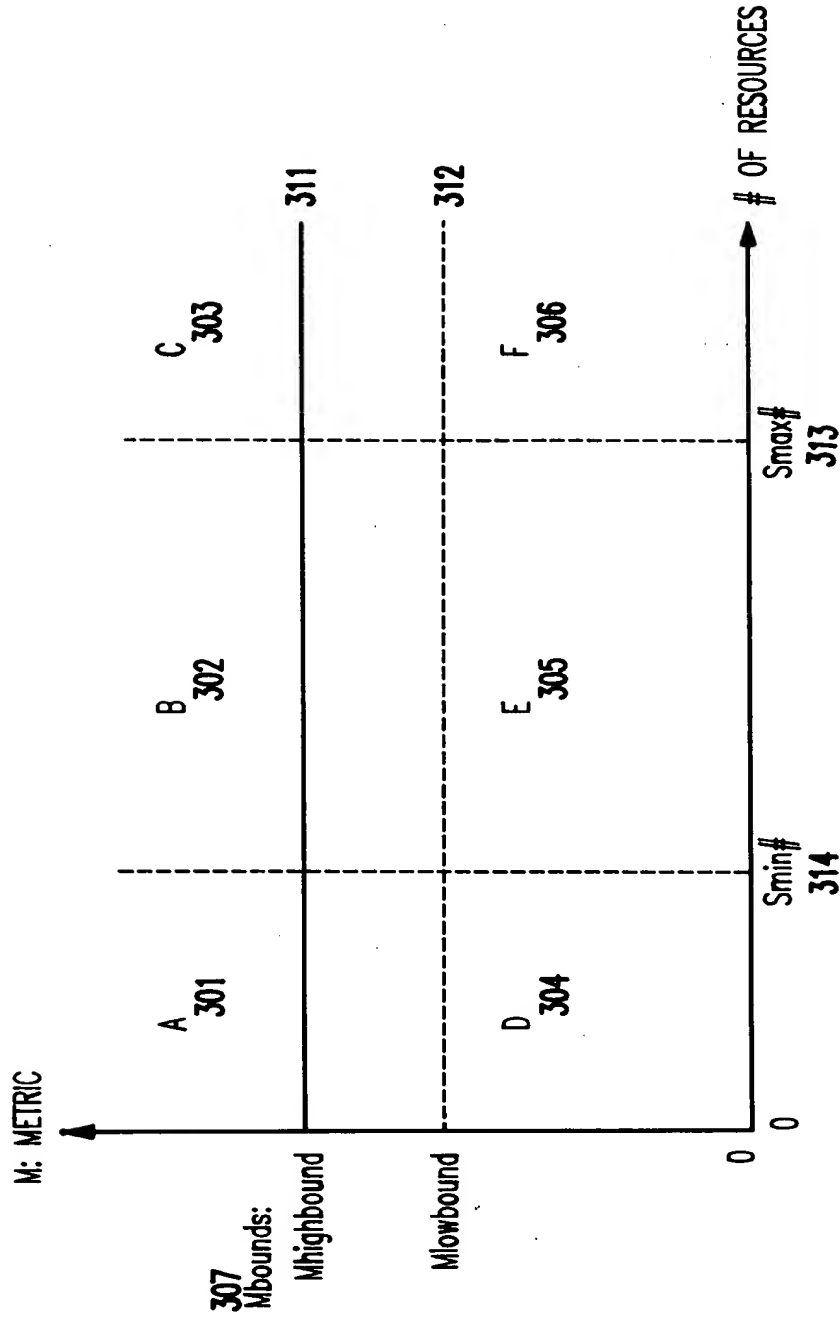


FIG.3

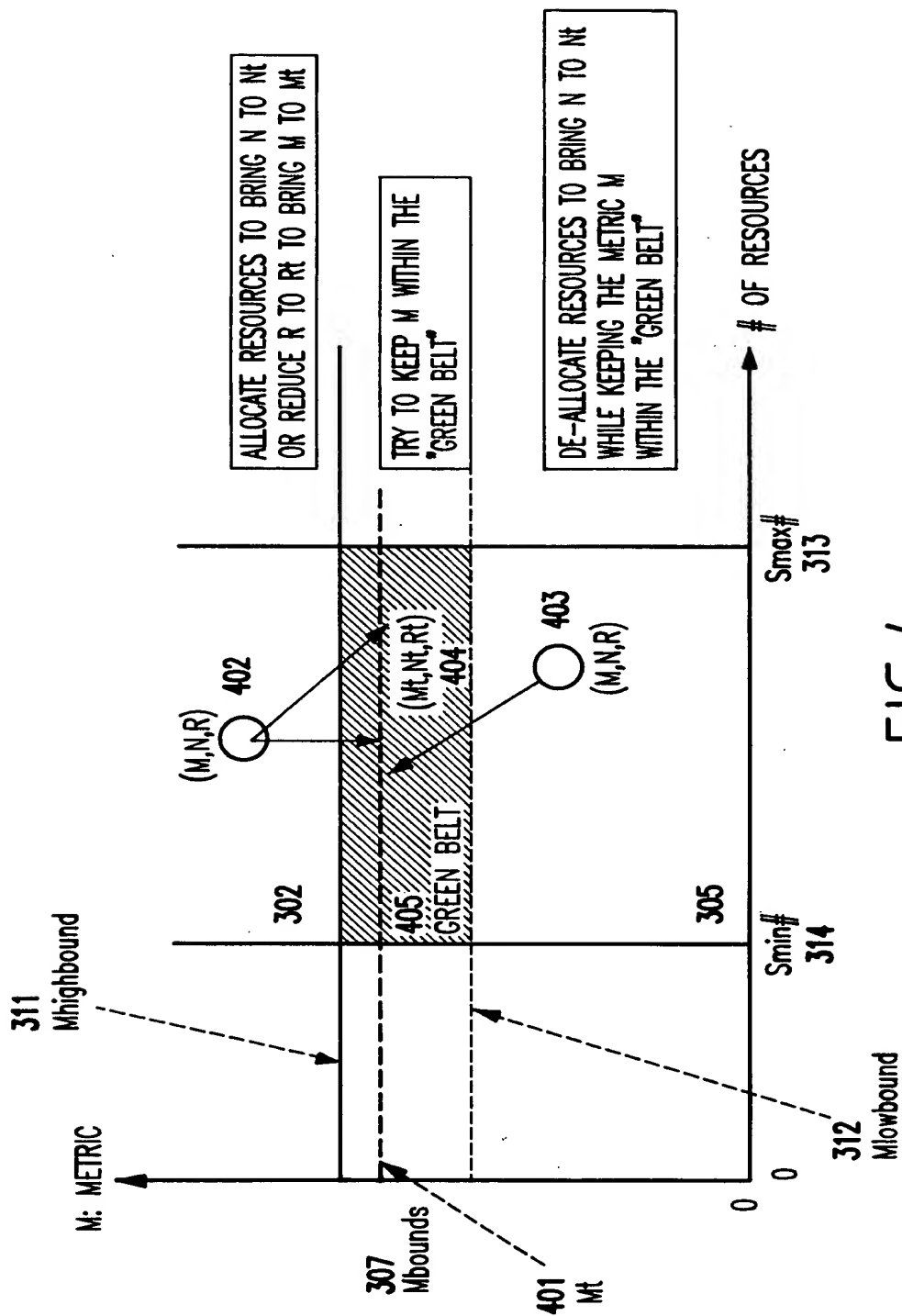


FIG.4

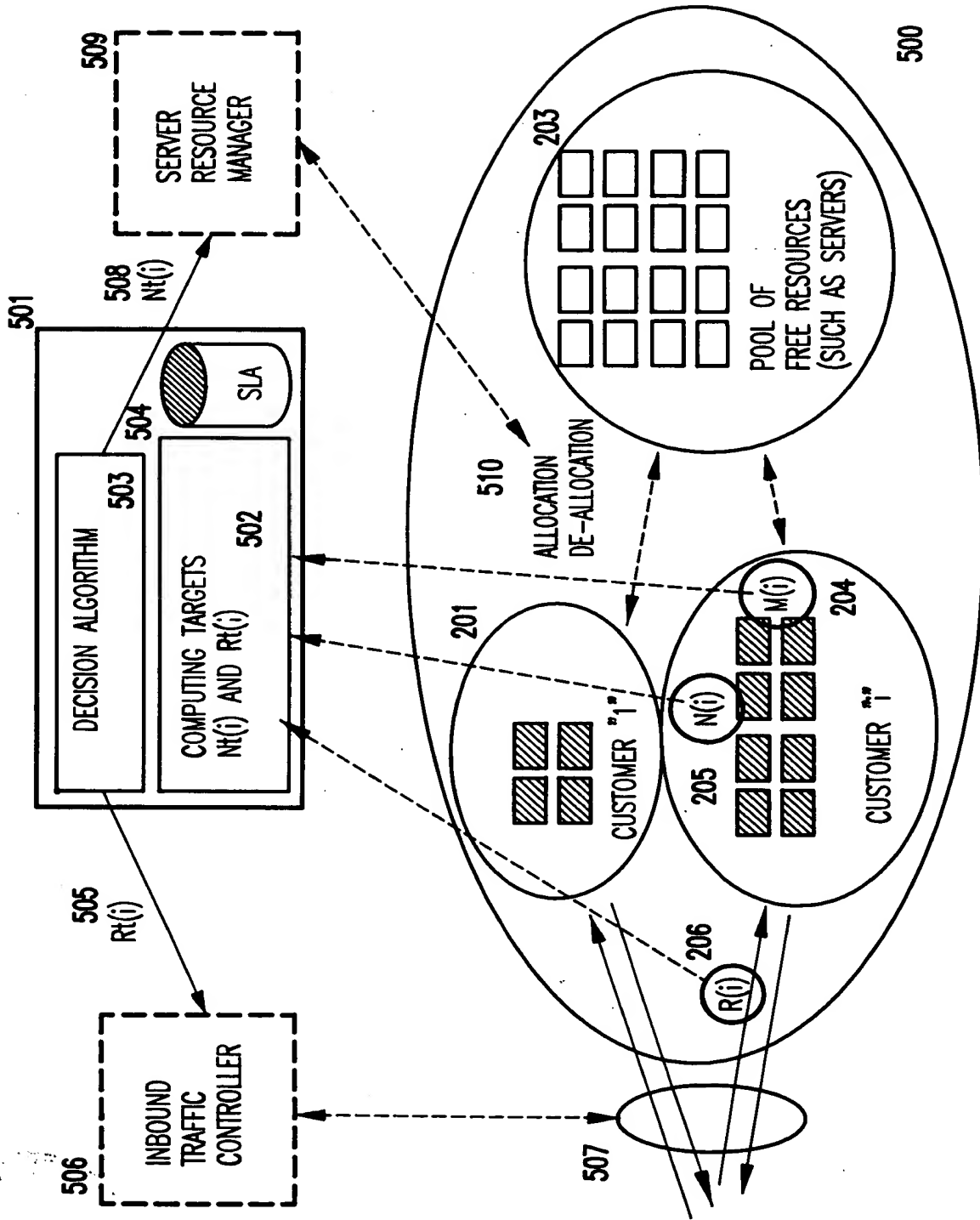


FIG. 5

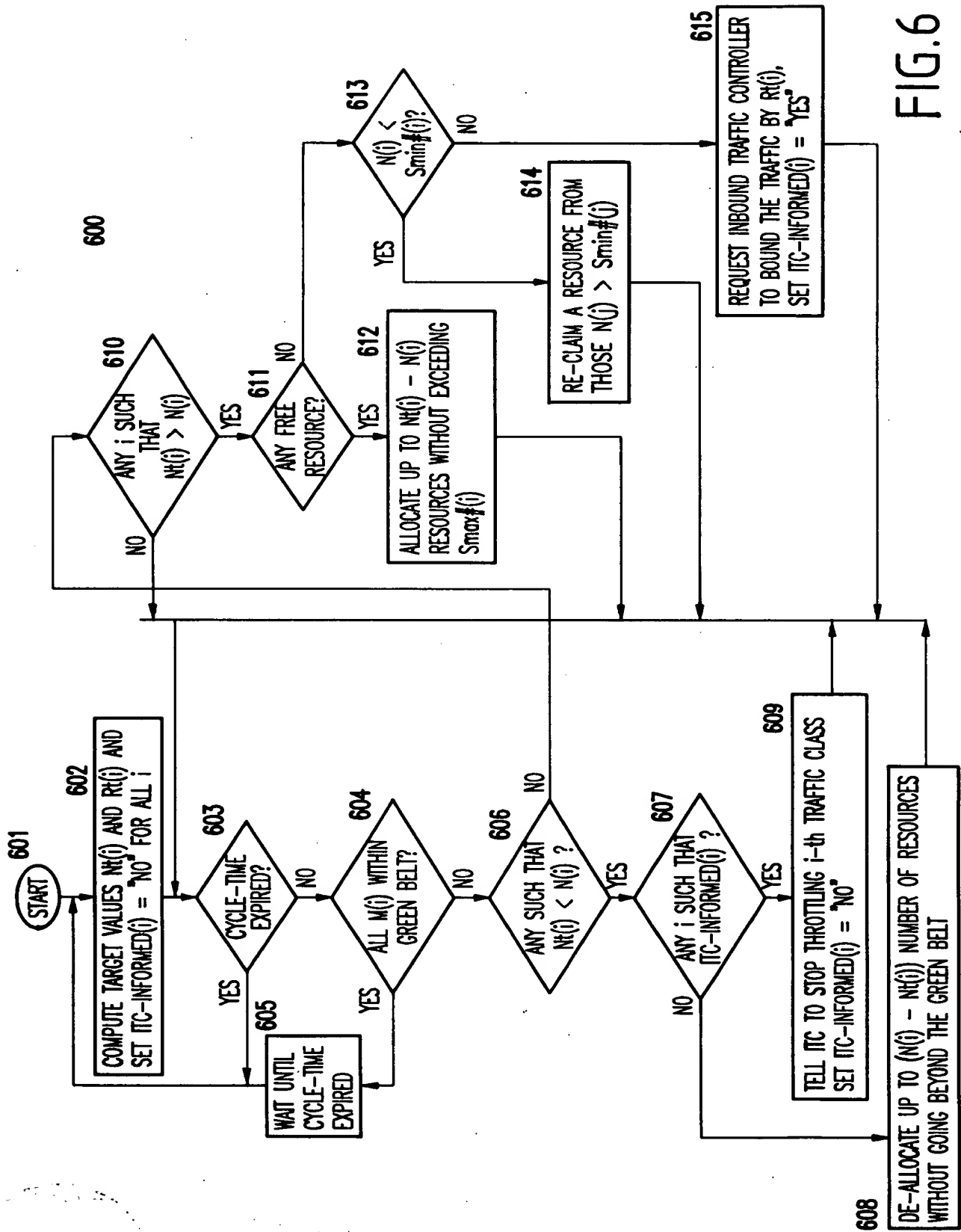


FIG.6

<b>Smin#(i)</b>	: the amount of resources guaranteed for the i-th customer. This can be a vector.
<b>Smax#(i)</b>	: the maximum amount of service resources that could be made available to the i-th customer. This can be a vector.
<b>Mbounds(i)</b>	: the bounds on the service level metric. Each "bounds" consists of a pair, "highbound" and "lowbound."
<b>Ubounds(i)</b>	: the bound on the utilization of resources allocated to the i-th customer
<b>Tbounds(i)</b>	: the bound on the agreed upon average server response time for the i-th customer
<b>T%bounds(i)</b>	: the bound on the agreed upon server response time percentile for the i-th customer
<b>(Smin#(i), Smax#(i), Mbound(i))</b>	: the SLA supported by the invention
<b>N(i)</b>	: the number (or amount of) of resources currently allocated to the i-th customer.
<b>R(i)</b>	: the current inbound traffic rate for the i-th customer. This could be a vector when more than one type of traffic is defined for each customer.
<b>M(i)</b>	: the current value of the metric M for the i-th customer. This could be a vector. Examples are: <b>U(i)</b> : the current utilization of the allocated resources to the i-th customer <b>T(i)</b> : currently observed server response time averaging for the i-th customer <b>T%(i)</b> : currently observed server response time percentile for the i-th customer
<b>Mt(i)</b>	: the "target" (want to achieve) metric value for the i-th customer. Its dimension is same as the dimension of M(i). This is within the defined "green belt" which is the region within which M(i) is kept. Examples of Mt(i) are: <b>Ut(i)</b> : the target resource utilization when M = U, <b>Tt(i)</b> : the target average response time when M = T <b>Tt%(i)</b> : the target percentile response time when M = T%

Table 1

**For Utilization as Metric:  $M = U$  and  $Mt = Ut$**

The following relationships hold among various variables:

$$U(i) = C(i)R(i) / N(i), \text{ where } C(i) \text{ is a constant}$$

$$Ut(i) = C(i)R(i) / Nt(i), \text{ and}$$

$$Ut(i) = C(i)Rt(i) / N(i).$$

From the above and from the given values of  $N(i)$ ,  $R(i)$ ,  $U(i)$ , and the target value  $Ut(i)$ ,  $Nt(i)$  and  $Rt(i)$  can be computed as follow:

$$Nt(i) = \text{CEILING} [N(i)U(i) / Ut(i)], \text{ and}$$

$$Rt(i) = \text{FLOOR} [R(i)Ut(i) / U(i)],$$

where CEILING gives the smallest integer exceeding and FLOOR gives the largest integer not exceeding.

**Table 2**

**For Average Response Time as Metric:  $M = T$  and  $Mt = Tt$**

**$S(i)$**  :server "service" (or processing) time for the  $i$ -th customer, this can be computed from observing each individual server service time, or estimated from a queueing formula:

**$S(i)$**  is a function of  $\{T(i), R(i), N(i)\}$

If the cluster of servers is modeled by the M/M/m queueing system,

$$S(i) = ((R(i)T(i) + N(i) + p\{N(i)\}) - \text{SQRT}((R(i)T(i) + N(i) + p\{N(i)\})^2 - 4R(i)T(i)R(i) / 2R(i)))$$

where  $p\{m\}$  is the probability that there are  $m$  requests in the  $i$ -th customer's server cluster

For the M/M/m queueing model,

$$Tt(i) \sim S(i) + p\{Nt(i)\}S(i) / (Nt(i) - R(i)S(i))$$

$$Tt(i) \sim S(i) + p\{N(i)\}S(i) / (N(i) - Rt(i)S(i))$$

Therefore,

$$Nt(i) = \text{CEILING} [R(i)S(i) + p\{Nt(i)\}S(i) / (Tt(i) - S(i))]$$

$$Rt(i) = \text{FLOOR} [N(i)S(i) - p\{N(i)\} / (Tt(i) - S(i))]$$

where  $p\{m\}$  is the probability that there are  $m$  requests in the customer's server cluster

**Table 3**



**For Percentile Response Time as Metric:  $M=T\%$  and  $Mt=Tt\%$**

If  $T\%(i) > T\%bound(i)$ , then the average response time  $T(i)$  needs to be reduced by  $(T\%(i) - T(i))$ . Therefore, for  $T\%(i)$  to approach  $T\%bound$ , the average response time target  $Tt(i)$  becomes:

$$Tt(i) = T(i) - (T\%(i) - T\%bound(i)).$$

For the M/M/m queueing model,

$$Tt(i) \sim S(i) + p\{Nt(i)\}S(i) / (Nt(i) - R(i)S(i))$$

$$Tt(i) \sim S(i) + p\{N(i)\}S(i) / (N(i) - Rt(i)S(i))$$

and thus,

$$Nt(i) = \text{CEILING} [R(i)S(i) + p\{Nt(i)\}S(i) / (Tt(i) - S(i))] ]$$

$$Rt(i) = \text{FLOOR} [N(i)/S(i) - (p\{N(i)\}/Tt(i) - S(i))] ]$$

where  $p\{m\}$  is the probability that there are  $m$  requests in the customer's server cluster

**Table 4**

**For any given metric  $M$ ,**

There are quick simulation tools, quick numerical computation tools and other approximation formula are available in computing  $Nt(i)$  and  $Rt(i)$  from given (i.e., measured) values of  $R(i)$ ,  $N(i)$  and  $M(i)$ .

**Table 5**